## PARALLELIZING THE FAST MULTIPOLE METHOD USING A TASK-BASED RUNTIME FOR HETEROGENEOUS ARCHITECTURES

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A high performance implementation of the fast multipole method (FMM) is crucial of the numerical simulation of many physical problems [4]. In a previous study [3, 2, 1], we have shown that a task-based FMM formulation (i.e., using a direct acyclic graph representation of the computation) provides the flexibility required to process a wide spectrum of particle distributions efficiently on multicore architectures. In this talk, we will show how such an approach can be extended to fully exploit heterogeneous platforms. For that, we designed highly tuned GPU versions of the two dominant operators (P2P and M2L) as well as a scheduling strategy that *dynamically* (i.e., at runtime) decides which tasks get processed on regular CPU cores and on GPU accelerators. We assessed our method with the StarPU runtime system for executing the resulting task flow. The platform is an Intel X5650 Nehalem multicore processor possibly enhanced with one, two or three Nvidia Fermi M2070 or M2090 GPUs. A detailed experimental study on two 30 million particle distributions (a cube and an ellipsoid) show that the resulting software consistently achieves high performance across various parallel processor architectures.

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