

## FATIGUE CRACK PROPAGATION AND THEIR INTERACTION MODELLING WITH A PERIDYNAMICS APPROACH

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In different fields of human activities structural components have to be in use, despite ageing and the continuous risk of damage growth and consequent possible failure. The modelling of damage propagation phenomena is usually a difficult task because it is necessary to have the capability of describing generation and growth of material discontinuities. For structural components, it is of the highest importance to be able to describe the damage process in order to evaluate their life expectancy for a safe use and to define a proper repair and maintenance program.

In the last thirty years some approaches have been proposed to deal with discontinuities in structural materials: interface elements and Cohesive Zone Models (CZM) [1] can only be applied if the path of the discontinuity is known a priori and it is limited by the element discretization; the extended finite element method (XFEM) [2] is more recent and, although overcoming some of the CZM drawbacks, its extension to 3D problems appears to be rather complex [3]. Recently a powerful method based on the peridynamic theory [4] has been introduced; the peridynamic equation of motion is formulated using spatial integral equations. The integral equations remain valid at discontinuities which enables to model crack initiation and propagation in a natural way even when cracks take place simultaneously at multiple locations. The theory is also able to predict crack branching and mutual crack interaction without any special additional criteria. The peridynamic theory is therefore a natural approach for the study of fatigue failure phenomena.

So the peridynamic formulation has been enriched introducing a damaging effect due to the high cycle fatigue phenomena, this formulation is inspired by previous work reported in references [5, 6].

The main parameters of the fatigue damage model are the material fatigue parameters and the number of the load cycles. It is possible also to simulate complex load history with many load cycle blocks with different applied stress value [7].

For the numerical implementation an incremental approach has been adopted, the number of cycles will be considered as a real-valued variable and a rate-independent model is assumed. The solution, including the bond fatigue damaging effect, is found using a standard Newton-Raphson technique.

A first study of the correlations between the peridynamic fatigue model parameters and the classical Paris law parameters has been presented on [8].

A distinguishing feature of this approach is its ability to treat the spontaneous formation of discontinuities at different locations together with their mutual interaction and growth in a consistent framework. The method does not require a separate crack growth law to be provided that governs cracks and damage initiation, growth, arrest, branching and so on: these features emerge from the equation of motion and constitutive models.

The peridynamic method will be applied to model a 2D structure in presence of voids and inclusions under fatigue load conditions considering isotropic materials. Results will be evaluated taking into account different mesh sizes, horizon dimensions, crack initial lengths and crack orientations.

## REFERENCES

- [1] Y. Mi, M. A. Crisfield, G. A. O. Davies, H. B. Hellweg, Progressive delamination using interface elements, *J Compos Mater*, Vol **32**, pp. 1246-1272, 1998.
- [2] G. Zi, T. Belytschko, New crack-tip elements for XFEM and applications to cohesive cracks, *Int J Numer Meth Eng*, Vol. 57, pp. 2221-2240, 2003.
- [3] N. Möes, C. Stolz, N. Chevaugeon, A. Salzman, The Thick Level Set Model: A non-local damage model allowing automatic crack placement inside localization zones, *Proceedings of CFRAC 2013, Computational Modeling of Fracture and Failure of Materials and Structures*, 5-7 June, Prague, Czech Republic, 2013.
- [4] S.A. Silling, Reformulation of elasticity theory for discontinuities and long-range forces, *J. Mech. Physics Solids*, Vol. **48**, No. 1, pp. 175-209, 2000.
- [5] R. H. J. Peerlings, W. A. M. Brekelmans, R. de Borst and M. G. D. Geers, "Gradient-enhanced damage modelling of high-cycle fatigue", *Int. J. Num. Meth. Engin.*, Vol. **49**, No 12, pp. 1547–1569, 2000.
- [6] Galvanetto U., Robinson P., et. al., A Simple Model for the Evaluation of Constitutive Laws for the Computer Simulation of Fatigue-Driven Delamination in Composite Materials, *SDHM*, Vol. **5**, No. 2, pp. 161-189, 2009.
- [7] M. Zaccariotto and U. Galvanetto, "Modeling of Fatigue Crack Propagation with a Peridynamics Approach", *8th European Solid Mechanics Conference*, 9-13 July, Graz, Austria, 2012.
- [8] M. Zaccariotto, F. Luongo, G. Sarego, D. Dipasquale and U. Galvanetto, Fatigue Crack Propagation with Peridynamics: a sensitivity study of Paris law parameters, *CEAS2013: "Innovative Europe"*, 16-19 September, Linköping, Sweden, 2013.