

## Modeling and control of ferromagnetic nanowires

Yannick Privat<sup>1</sup> and Emmanuel Trélat<sup>2</sup>

<sup>1</sup> IRMA, Université de Strasbourg, CNRS UMR 7501, Inria, 7 rue René Descartes, 67084 Strasbourg, France ([yannick.privat@unistra.fr](mailto:yannick.privat@unistra.fr)). Institut Universitaire de France (IUF).

<sup>2</sup> Sorbonne Université, CNRS, Université de Paris, Inria, Laboratoire Jacques-Louis Lions (LJLL), F-75005 Paris, France ([emmanuel.trelat@sorbonne-universite.fr](mailto:emmanuel.trelat@sorbonne-universite.fr)).

**Keywords:** *Landau-Lifshitz equation, control, stabilization.*

In this talk, we investigate the problem of modeling and controlling finite-length ferromagnetic nanowire, in which the evolution of the magnetization vector is governed by the Landau-Lifshitz equation. We first provide a description of all steady-states of this equation and study their local stability properties. In particular, a quantization property in terms of a certain energy will be highlighted. Then we address the problem of controlling and stabilizing steady-states by means of an external magnetic field induced by a solenoid rolling around the nanowire. We prove that, for a generic placement of the solenoid, one can steer approximately the system from any steady-state to any other one, provided that they have the same energy level. The proof of this result rests upon the investigation of local exponential stabilization properties of the Landau-Lifshitz equation with a feedback control.

## REFERENCES

- [1] G. Carbou, S. Labb  . Stabilization of walls for nano-wires of finite length. *ESAIM Control Optim. Calc. Var.* 18 (2012), no. 1, 1–21.
- [2] S. Labb  , Y. Privat, E. Tr  lat. Stability properties of steady-states for a network of ferromagnetic nanowires. *J. Differential Equations* 253 (2012), no. 6, 1709–1728.
- [3] Y. Privat and E. Tr  lat. Control and stabilization of steady-states in a finite-length ferromagnetic nanowire. *ESAIM Control Optim. Calc. Var.* 21 (2015), no. 2, 301–323.