

## Reduced Arlequin Coupling Operators For Solution of Localized-HF Multiscale Dynamic Problems

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**Keywords:** *Multiscale, Dynamic, Reduced Volume Coupling, Arlequin Framework*

A numerical solution of localized High-Frequency dynamic multiscale problems, previously introduced in [1] (see also [2]) and recently pushed farther in [3], form the backbone of the present communication. Some application for the resulting approach are modeling and solution of waves propagating from a first critical High Frequency zone of interest, denoted,  $(Zoi)_{HF}$ , neighborhood of a seismic-like source (e.g. earthquake, impact, fracturation, etc.) to, say, a Low-Frequency  $2^{nd}$  critical zone  $(Zoi)_{LF}$ , located significantly far from the  $(Zoi)_{HF}$ , while coarsely considering damping of the propagating medium. Considering an earthquake, one can imagine that a global refinement of the whole domain, with distance between the seismic source and the infrastructure of the order of tens of  $Km$  or more is out of reach for any reasonable computer. Multiscale dynamic methods are thus required. The Arlequin framework initiated in [5] is used herein. The main addressed points in this work are i) when and how one can justify localized HF hypotheses and why the characteristic volume-Arlequin coupling is essential for transient multiscale dynamic problems. ii) A presentation of new reduced characteristic Arlequin-volume-coupling operators, based on "consistent physical pairing" of fine and coarse Lagrange Arlequin multipliers. iii) How to avoid the pollution of  $(Zoi)_{HF}$  while transmitting the maximum possible of energy to  $(Zoi)_{LF}$ . Enlightening numerical tests are shown during the conference.

## REFERENCES

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