

# A nonlinear subgrid drift velocity model for filtered drag in turbulent fluidization

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Small-scale turbulent topologies get highly complicated when merging into multiphase flows. For instance, when a turbulent flow pulls small inertia particles in a particle-laden turbulence, the particles at low mass loading drain kinetic energy from the carrier fluid and produce a kind of relaminarization. While, at significantly large mass loading, the particles get self-organized into dense clusters triggering a drag production and momentum feedback on the carrier-fluid, and enhance its turbulent kinetic energy as *cluster-induced turbulence (CIT)*. This drag production or CIT is relatively expressed by the subgrid-scale (SGS) drift velocity  $\mathbf{v}_d$  on mesoscale description (*i.e.* spatially filtered coarse grid). Considering a gas-particles turbulent fluidization simulated in the framework of two-fluid model (TFM); the most classical closure for  $\mathbf{v}_d$  assumes that  $\mathbf{v}_d^{model}$  is linearly aligned against the resolved gradient of solid volume fraction  $\bar{\epsilon}_s$ , with a scalar turbulent dispersion  $D_{tg}$ , *i.e.*  $\mathbf{v}_d^{Bur} \sim D_{tg} \nabla \bar{\epsilon}_s / (\bar{\epsilon}_s \bar{\epsilon}_g)$  [1], where  $\bar{\epsilon}_g$  is the gas-phase volume fraction. Recently and on the base of our novel analysis of small-scale structures in dense turbulent fluidization [2], the linear model  $\mathbf{v}_d^{Bur}$  has revealed a clear misalignment with the actual  $\mathbf{v}_d^A$  due to the (strong tendency) boundary-layer-like turbulence on the gas-phase. This leads us in the current work to derive and explore the behaviour of a new proper nonlinear model basing on non-negative clipping (regularized) rate-of-strain gas-phase tensor and solids gradient, *i.e.*  $\propto \bar{\mathbf{S}}_g^\oplus \nabla \bar{\epsilon}_s / (\bar{\epsilon}_s \bar{\epsilon}_g)$ , where,  $\bar{\mathbf{S}}_g = 1/2(\bar{\mathbf{G}}_g + \bar{\mathbf{G}}_g^t)$ , and  $\bar{\mathbf{G}}_g = \bar{\epsilon}_s [\nabla \bar{\mathbf{u}}_s - 1/3 \text{tr}(\nabla \bar{\mathbf{u}}_s) \mathbf{I}]$  (similar to the framework of LES models).

## REFERENCES

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