

A Virtual Element Method For Phase Field Modeling of Brittle Fracture

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An efficient low order **virtual element formulations** that account for isotropic brittle failure response in two-dimensional case is outlined within this work. The modeling of crack formation can be achieved in a convenient way by continuum **phase-field** approaches to fracture, which are based on the regularization of sharp crack discontinuities as rooted in [1,2]. This avoids the use of complex discretization methods for crack discontinuities, and can account for complex crack patterns.

In the presented contribution, the *recently developed* virtual element method (VEM) will be used, because of the flexible choice of nodes number in an element which can be changed easily during the simulation process, as addressed in [3,4]. To this end, the potential energy is formulated in terms of *suitable polynomial functions*, instead of computing the unknown shape functions for complicated element geometries, e.g. arbitrary convex or concave polygonal elements.

The modeling capabilities and algorithmic performance of the proposed formulation is demonstrated by a number of numerical examples.

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