On the Stability of Explicit and Implicit Co-Simulation Approaches

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Abstract

Applying a co-simulation approach [2], the numerical stability of the coupling method is a crucial point. In the framework of this paper, we consider explicit and implicit co-simulation approaches. The two subsystems are assumed to be coupled by constitutive equations, i.e. we consider the case that the subsystems are connected by applied forces/torques [1, 3]. Coupling approaches based on algebraic constraint equations are not considered here.

The numerical stability of time-integration schemes is defined by Dahlquist's test equation. From the mechanical point of view, this equation can be interpreted as the complex representation of the equations of motion of the autonomous linear mass-spring-damper oscillator. For analyzing the stability of co-simulation methods, an appropriate test model has to be defined. Considering coupling methods based on constitutive equations, the most useful choice is the two-mass oscillator shown in Figure 1. This 2-DOF oscillator can be regarded as two single-mass oscillators (masses m_1/m_2 , spring constants c_1/c_2 , damping coefficients d_1/d_2), which are coupled by the coupling spring c_c and the coupling damper d_c . Therefore, the two-mass oscillator can be considered as two Dahlquist equations, which are coupled by a linear spring/damper system.



Figure 1: Test model for analyzing the stability of co-simulation methods: Linear two-mass oscillator.

Introducing dimensionless variables, it can be shown that the co-simulation test model is described by seven independent parameters. By discretizing the co-simulation test model with a linear co-simulation approach, a linear recurrence equation system can be derived, which describes the time discrete solution of the co-simulation approach [4]. The stability of the co-simulation method can easily be determined by calculating the spectral radius of the recurrence equation system. In the paper, stability plots are presented as a function of the seven test-model parameters. Different co-simulation techniques are compared with respect to their numerical stability.

References

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