

# EFFECT OF VISCOSITY ON THE ROBUSTNESS OF THE ELEMENT DELETION METHOD FOR CRACK PROPAGATION MODELLING

C. Canales\* and J.-P. Ponthot

University of Liège, Department of Aerospace & Mechanical Engineering  
Chemin de chevreuils 1, 4000 Liège, Belgium  
{CCanales, JP.Ponthot}@ulg.ac.be

**Key words:** *Finite Element Method, Crack propagation, Element deletion method, Viscoplasticity.*

The numerical simulation of crack propagation in solids is of main importance in fracture mechanics and has been extensively studied over the years. Several approaches have been developed in order to describe the evolving geometry of a crack [1–6], but despite the research efforts some challenges are still present. A commonly used technique in Finite Element codes is the element deletion method due to the simplicity of its numerical implementation and possible extension to 3D. Furthermore, it is possible to couple this method with any failure criterion or damage model without additional considerations. This advantages are extremely desirable for numerical approaches involving high computational costs, e.g. the multi-scale computational homogenization [7, 8], where the element deletion method can be used at the micro-scale to simulate the nucleation, growth and coalescence of micro-voids [9].

In this work, the effect of viscosity on the numerical response of the element deletion method is studied. The selected elastic-viscoplastic model corresponds to an extension of Perzyna’s model, for large strains [10]. The onset for the initiation of crack and further propagation steps through metallic materials are driven by a damage model. Two benchmark tests are selected to evaluate the robustness of the method. The first test under analysis is the Compact Tension test [11] applied to an aluminium specimen. In this case the crack propagation is dominated by a single mode of separation (mode I). The second test corresponds to a steel plate under tension with two notches asymmetrically positioned in opposite corners of the specimen, resulting in a more complex state of stress. The effect of constitutive parameters governing the viscous part of the behavior is considered to study the reliability of the solution along with the discretization and failure criterion. The results were compared with those reported in [4], where a remeshing approach was adopted to model crack propagation.

## References

- [1] G.T. Camacho and M. Ortiz. Computational modeling of impact damage in brittle materials. *Int. J. Solids Struct.*, Vol. **33**, 2899–2938, 1996.
- [2] J.C. Simo and M.S. Rifai. A class of mixed assumed strain methods and the method of incompatibles modes. *Int. J. Numer. Methods Eng.*, Vol. **29**, 1595–1638, 1990.
- [3] J. Oliver. Modelling strong discontinuities in solid mechanics via strain softening constitutive equations. Part 1: fundamentals. *Int. J. Numer. Methods Eng.*, Vol. **39**, 3575–3623, 1996.
- [4] J. Mediavilla, R.H.J. Peerlings and M.G.D. Geers. A robust and consistent remeshing-transfer operator for ductile fracture simulations. *Comput. Struct.*, Vol. **84**, 604–623, 2006.
- [5] T. Belytschko and J. Lin. A three-dimensional impact-penetration algorithm with erosion. *Comput. Struct.*, Vol. **25**, 95–104, 1987.
- [6] N. Moës, J. Dolbow and T. Belytschko. A finite element method for crack growth without remeshing. *Int. J. Numer. Methods Eng.*, Vol. **46**, 131–150, 1999.
- [7] J. Fish, K. Shek, M. Pandheeradi, and M. S. Shephard. Computational plasticity for composite structures based on mathematical homogenization: Theory and practice. *Comput. Meth. Appl. Mech. Eng.*, Vol. **148**, 53–73, 1997.
- [8] V. Kouznetsova, W. A. M. Brekelmans and F. P. T. Baaijens. An approach to micro-macro modeling of heterogeneous materials. *Comput. Mech.*, Vol. **27**, 37–48, 2001.
- [9] L. Mishnaevsky, U. Weber and S. Schmauder. Numerical analysis of the effect of microstructures of particle-reinforced metallic materials on the crack growth and fracture resistance. *Int. J. Fract.*, Vol. **125**, 33–50, 2004.
- [10] J.P. Ponthot. Unified stress update algorithms for the numerical simulation of large deformation elasto-plastic and elasto-viscoplastic processes. *Int. J. Plast.*, Vol. **18**, 91–126, 2002.
- [11] ASTM E399-06. Standard test method for linear-elastic plane-strain fracture toughness of metallic materials, 2006.