

## A SEMI-STRUCTURED METHOD FOR HIGH-ORDER CURVILINEAR MESHING

Joaquim Peiro<sup>\*1</sup>, David Moxey<sup>1</sup>, Menashe Hazan<sup>1</sup> and Spencer J. Sherwin<sup>1</sup>

<sup>1</sup> Department of Aeronautics, Imperial College London,  
South Kensington Campus, London SW7 2AZ, U.K.  
{j.peiro,d.moxey,menashe.hazan10,s.sherwin}@imperial.ac.uk

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The generation of high-order curvilinear meshes for complex geometries and high Reynolds numbers presents a challenge due to the requirement of generating elements in the boundary layers that are stretched in the direction of the flow with ratios of 1000 to 1 or higher.

Generating this type of high-order meshes is difficult for approaches based on elasticity that globally curve a linear boundary conforming mesh by projecting additional points in the linear mesh, project the boundary nodes on the boundary onto the curved surface and deform the mesh to accommodate them [1, 3] or alternatively undertake expensive optimization to untangle it [2].

The idea that we present is conceptually simple but very effective and modular since it permits the generation of a sequence of meshes with increased resolution with very little additional cost which should prove very valuable for mesh convergence studies at high Reynolds numbers. We propose an isoparametric approach [4] where a mesh that contains a valid coarse discretisation into high-order triangular prisms of the boundary layer is subdivided to obtain a finer prismatic or tetrahedral boundary-layer mesh. The validity of the prismatic mesh provides a suitable mapping that, with a careful choice of the element shape functions, permits to obtain very fine mesh resolutions across the thickness of the boundary layer.

Figure 1 provides an illustration of the procedure. The initial coarse mesh that contains large triangular prismatic elements in the boundary-layer region is depicted in Figure 1(a). The prismatic elements are split long the normal to obtain a finer discretization, shown in Figure 1(b), which is suitable for the representation of viscous flows at high Reynolds numbers. If a full tetrahedral mesh is required, the prismatic mesh is split into tetrahedral elements leading to the mesh of Figure 1(c).

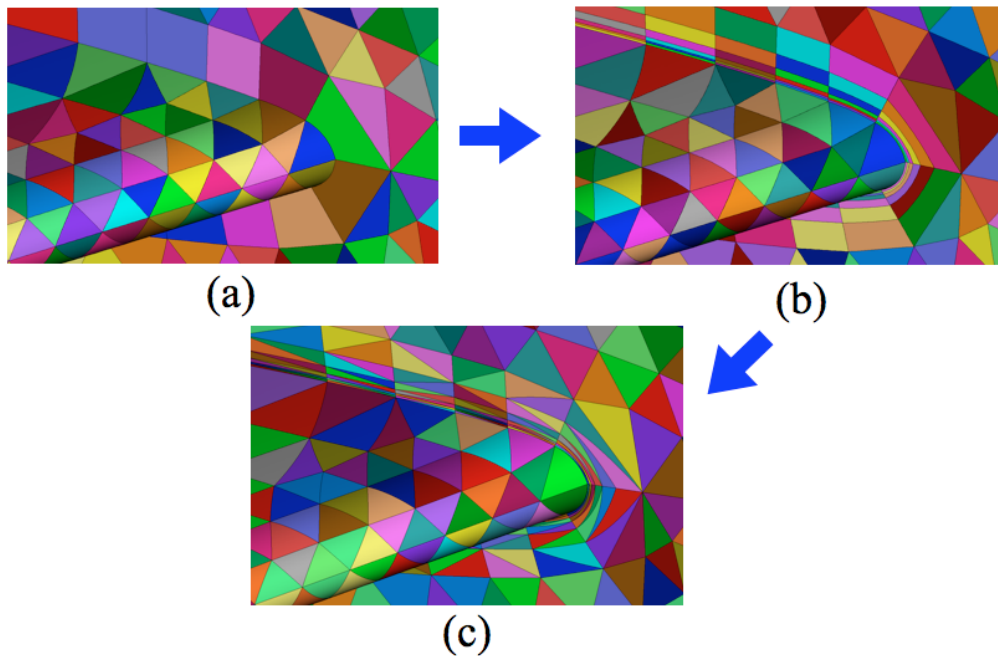


Figure 1: An illustration of the proposed procedure: (a) initial coarse mesh; (b) split of the boundary layer prisms in the direction normal to the boundary; and (c) the prismatic mesh is subdivided to obtain a fully tetrahedral mesh.

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