

## AN EFFICIENT TECHNIQUE BASED ON NUMERICAL MODE MATCHING FOR THE ACOUSTIC CHARACTERIZATION OF DISSIPATIVE SILENCERS WITH THERMAL GRADIENTS

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In this work, a computationally efficient numerical technique based on the mode matching method is presented to model and analyse the acoustic behaviour of dissipative silencers. Three-dimensional wave propagation and temperature gradients are considered in the absorbent material while a perforated duct separates the dissipative region and the central passage. The use of a full multidimensional finite element formulation is computationally expensive in configurations with arbitrary geometry and complex thermal gradients [1]. To avoid this drawback, a technique is proposed combining axial and transversal solutions of the wave equation in the different ducts. The latter are obtained through a two-dimensional finite element approach that allows the computation of the eigenvalues and eigenvectors associated with the transversal section [2], including radial temperature gradients and the corresponding thermal-induced heterogeneities of the absorbent material properties [3]. Due to the reduced acoustic impact of axial gradients compared to radial variations [1], an axially uniform temperature field is assumed, its value being the inlet/outlet average. Then, the compatibility equations of the acoustic field (pressure and axial acoustic velocity) at the geometric discontinuities together with the mode matching method [2] are used to obtain the wave propagation coefficients in the different regions of the silencer, such as the central chamber and the inlet/outlet pipes. This methodology is compared with the results given by full three-dimensional finite element computations including axial and radial temperature gradients, showing a good agreement with lower computational requirements.

### REFERENCES

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