A CONSISTENT FINITE ELEMENT APPROACH TO LARGE EDDY SIMULATION REVISITED WITH HIGHER-ORDER ELEMENTS II

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During the European project **ADIGMA** (Adaptive Higher-Order Variational Methods for Aerodynamic Application in Industry) Dassault Aviation extended its stabilized finite element industrial Navier-Stokes code AeTher to higher-order elements. The high-order approach (3^{rd} and 4^{th} order) was carefully assessed using inviscid subsonic and transonic, laminar, and high Reynolds number turbulent flows. First results on a full aircraft configuration were also achieved [3]. They showed that spurious drag was considerably reduced by the use of higher-order elements.

In this paper, we focus on the application of higher-order elements to Large Eddy Simulation. We revisit the results of [1] where a careful second-order accurate LES model was introduced. At that time we established that second-order accuracy was sufficient for the practical utilization of LES in the industry. Today the industrial applications of LES and DES are numerous (see [2] and Fig. 1). We reconsider the use of these models in the light of higher-order elements, possibly reducing the number of grid points required per wave length and increasing the number of resolved scales for a given grid size.

We reconsider the DES of the flow past the QinetiQ M219 open cavity at a transonic Mach number. In Figure 2, we compare the results obtained with the original secondorder accurate linear elements against third-order accurate quadratic elements. In both instances time integration is provided by a standard second-order accurate backward difference scheme. Both meshes contain the exact same number of degrees of freedom. One can notice a more rapid transition to 3-D flow and finer turbulent structures in the higher-order solution. Early analysis suggests that higher-order elements reveal the limits of simple subgrid-scale models, such as the underlying Smagorinsky model in DES, in a stronger way than mesh refinement with standard second-order elements. The impact of a selective Smagorinsky model is shown in the light of higher-order elements. Additional gain is expected with higher-order time integration combined with quadratic or cubic elements.



Figure 1: Turbulent structures behind the leading-edge slat of a high-lift configuration.

Figure 2: Turbulent structures in the QinetiQ M219 cavity: standard 2nd-order linear P1 elements (left) vs. 3rd-order quadratic P2 elements (right).

REFERENCES

- F. Chalot, B. Marquez, M. Ravachol, F. Ducros, F. Nicoud, and T. Poinsot, "A consistent Finite Element approach to Large Eddy Simulation," paper #98-2652, 29th AIAA Fluid Dynamics Conference, Albuquerque, NM, June 15–18, 1998.
- [2] F. Chalot, V. Levasseur, M. Mallet, G. Petit, and N. Réau, "LES and DES simulations for aircraft design," paper #2007-0723, 45th AIAA Aerospace Sciences Meeting and Exhibit, Reno, NV, January 8–11, 2007.
- [3] F. Chalot and P.-E. Normand, "Towards high-fidelity industrial CFD," 5th ECCOMAS European Conference on Computational Fluid Dynamics, Lisbon, Portugal, June 14– 17, 2010.

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