

REDUCED COLLOCATION METHODS WITH PARAMETRIC PRECONDITIONING

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In this talk, we present a reduced basis (RB) method well-suited for the collocation framework [1] together with parametric preconditioning techniques [2] for the resulting *reduced collocation method*. These works provide stable and efficient reduced basis strategies to practitioners who prefer a collocation, rather than Galerkin, approach. Two fundamentally different RB algorithms will be presented. One of these two algorithms eliminates a potentially costly online procedure that is needed for non-affine problems with Galerkin approach. The preconditioner can be parameter dependent and have the traditional affinity with respect to the parameters which allows for an offline-online decomposition. It improves the quality of the error estimation uniformly on the parameter domain, and speeds up the convergence of the reduced solution to the truth approximation significantly. Numerical results will also be presented to demonstrate the high efficiency and accuracy of these approaches.

REFERENCES

- [1] Y. Chen and S. Gottlieb. Reduced collocation methods: Reduced basis methods in the collocation framework. *J. Sci. Comput.*, 55(3): 718–737, 2013.
- [2] Y. Chen and S. Gottlieb and Y. Maday Parametric preconditioning and its applications to Reduced Collocation Methods. *To be submitted.*