

A projection hybrid FV/FE method for low Mach number flows

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The scope of this talk is to extend the projection hybrid finite volume/finite element method introduced in [1] and [2] to solve compressible low Mach number flows. Starting with a 3D tetrahedral finite element mesh, the momentum equation is discretised by a finite volume method associated with a dual finite volume mesh. A variation on the classical flux function defined by Rusanov scheme is proposed in order to avoid the spurious oscillations originated by the time and space dependency of the density. To attain second order schemes CVC-Kolgan and LADER methodologies are considered (see [4] and [3]). The Galerkin approach used for the computation of the gradients involved in the diffusion term reduces the stencil and the computational cost of the transport-diffusion stage. Concerning the projection stage, the pressure correction is computed by a piecewise linear finite element method associated with the initial tetrahedral mesh. Finally, several test problems are presented to assess the performance of the method.

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