A NITSCHE FINITE ELEMENT METHOD FOR THE NAVIER-STOKES EQUATIONS WITH SLIP CONDITIONS ON CONFORMING INTERNAL INTERFACES

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Slip velocity boundary conditions (BCs) can be used to simulate the effect of turbulent boundary layers in fluid-rigid body interaction models [1] and have been applied successfully in many applications in aerodynamics. To prescribe the slip boundary conditions we need to enforce the continuity of the velocity normal to the fluid-rigid body interface, while allowing a jump in the tangential velocities. Our aim is to extend this work to fluid-structure interaction (FSI) to allow for some important phenomena such as bending and vibration. A unified continuum fluid-structure interaction model [2] was developed to simulate flexible structures but with no slip boundary conditions imposed implicitly through the model. Here we investigate an extended finite element method [3] which allows for imposing slip boundary conditions over the internal fluid-structure interface. In the following figure we show preliminary results for inviscid flow past a rigid structure with no-slip BCs (left figure) and slip BCs (right figure) imposed at the internal interface. Only slip BCs can be used to describe the Euler flow correctly.

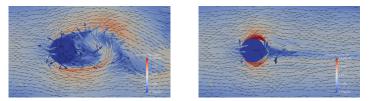


Figure: Euler flow approximated by a stabilized finite element method, with no slip (left) and slip (right) boundary conditions.

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