

# DISCONTINUITIES IN ISOGEOMETRIC ANALYSIS: INTERFACE ELEMENTS AND ENRICHED APPROACHES

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The  $C^0$ -based formulation of standard finite elements results in a jump in the derivatives, and subsequently in a poor estimate of the stresses across the element boundaries. The higher-order continuity provided in Isogeometric Analysis, which exploits B-splines and NURBS as basis functions, allows to remove this jump in the derivatives, and thus to produce of continuity also for the stress field [1]. The benefit of having a continuous, and therefore much more accurate stress field becomes important especially around crack tips, and Isogeometric Analysis can result in a superior stress calculation locally. This can yield an improved prediction of the onset of further crack propagation as well as of the direction of crack propagation. A drawback of Isogeometric Analysis is that it seems more limited to flexibly adapt the discretisation to the path of a freely propagating crack.

For cracks where the crack path is known a priori, interface elements have long been the method of choice. This is also the case for Isogeometric Analysis, and interface elements have also been developed within this framework [2, 3]. As an alternative to full remeshing and adaptivity, XFEM has been developed, and extended to Isogeometric Analysis, named XIGA [4, 5].

Herein, we set out to simulate crack propagation using Isogeometric Analysis via the two aforementioned approaches: isogeometric interface elements and XIGA. Regarding the latter, a succinct summary of the XFEM formulation is presented as an overture to XIGA, followed by a discussion of some numerical aspects of XIGA. The paper is concluded with examples of comparisons between both approaches.

## REFERENCES

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