A finite element formulation for non-Newtonian fluid flow through cracked, deformable porous media

Tim Hageman¹ and René de $Borst^2$

- ¹ Department of Civil and Structural Engineering, University of Sheffield, Sir Frederick Mappin Building, Mappin Street, S1 3JD, Sheffield, UK, thageman1@sheffield.ac.uk
- ² Department of Civil and Structural Engineering, University of Sheffield, Sir Frederick Mappin Building, Mappin Street, S1 3JD, Sheffield, UK, r.deborst@sheffield.ac.uk

Keywords: non-Newtonian, poroelasticity, fracture, finite elements

Non-Newtonian fluid flow through deformable porous materials is important in several common situations: for instance blood flow through the human body or flow of oil through fractured porous materials.

In order to accurately simulate these flows in the presence of cracks, a finite element formulation for non-Newtonian power-law fluids based on the generalized Darcy's law [1] [2] is derived. This formulation is appended with a subgrid model to include the effects of non-Newtonian fluid flow through cracks, formulated in a similar manner as was done by [3] for Newtonian fluids. This formulation was compared with several analytical and numerical solutions for Newtonian fluids and verified for non-Newtonian fluids with results from the built-in MATLAB solver.

The resulting code was used to simulate some typical boundary value problems. The results of this show the influence of the non-Newtonian behaviour on the pressure distribution in the fluid and deformations of the porous material.

References

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