## Identifying optimal meshes for high-order implicit large-eddy simulation of turbulent boundary layers using Kriging surrogate models

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This study aims to construct a framework to identify, a priori, grid properties that achieve accurate prediction of turbulent boundary layers when performing implicit large-eddy simulations (ILES) with high-order Flux Reconstruction (FR) schemes [1, 2]. Wall-normal cell distribution is defined by two parameters,  $\alpha$  and  $\beta$ , where  $\alpha$  determines the minimum wall-normal cell size adjacent to the wall, and  $\beta$  determines the expansion ratio of cell sizes in the wall-normal direction. An extensive parametric study is carried out in  $\alpha\beta$ -space on a turbulent plane Couette flow ( $Re_{\tau} = 171$ ) for various polynomial orders (p) and total degrees of freedom (DoF). Three cost functions are defined ( $J_1$ : log-layer mismatch;  $J_2$ : error in  $Re_{\tau}$ ; and  $J_3$ : allowable time-step size). A Kriging surrogate model of each cost function is then constructed in  $\alpha\beta$ -space, which provides a continuous map of computational accuracy and cost, with respect to wall-normal cell distributions for high-order FR schemes (Fig. 1). Finally, insights from the surrogate model are used to identify optimal meshing strategies for ILES of turbulent boundary layers with high-order FR schemes.

Fig. 1 Visualization of the optimal grid parameters that are identified from the overlap region (black dotted region) of  $\alpha\beta$ -combinations, where  $J_1$  and  $J_2$  are smaller than 30% of their maximum values and  $J_3$  is larger than 60% of its maximum value. Blue to white contours show the allowable



time-step size. The red star indicates the optimal grid parameters for maximizing the allowable time-step size in the overlap region.

## REFERENCES

- Huynh, H. T., A Flux Reconstruction Approach to High-Order Schemes Including Discontinuous Galerkin Methods, AIAA 2007-4079.
- [2] F. D. Witherden et al., PyFR: An open source framework for solving advection-diffusion type problems on streaming architectures using the flux reconstruction approach, Comput. Phys. Commun., Vol. 11, pp. 3028–3040, 2014.