A NEW DISCONTINUITY-DETECTING METHOD AND APPLYING TO CONSTRUCT 3RD-ORDER HYBRIDIZED WENO SCHEME

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Key Words: *Discontinuity-detecting method, hybridized WENO scheme, shock-capturing, complicated flow structures.*

Compared with WENO schemes, the hybridized WENO schemes have several advantages, such as the higher-order accuracy, lower numerical dissipation and higher efficiency. The performance of the hybridized schemes is determined mainly by the discontinuity detector. In this paper, a discontinuity detecting method for a four-point stencil, which is actually used in the third-order WENO scheme, is proposed and used to develop the high order accurate hybrid scheme of the third-order WENO scheme combining with a third-order compact upstream scheme. In order to demonstrate the advanced performance of the present detecting method, this paper also compares the schemes with the same hybrid form but using different detectors in references, the results show that, the hybrid scheme with the new method has least numerical dissipation, due to the new method can correctly treat the stencils containing critical points, while the others most possibly misjudge those stencils as discontinuous ones.

This work was supported by NKRDPC 2016YFA0401200, NSAF No. U1530145, SCP No.TZ2016002 and NSFC No.11272325.

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