

Optimal reconstruction of flows from doppler measurements.

Galarce F.¹, Gerbeau J.-F.¹, Lombardi D.¹, Mula, O.²

¹ Inria Paris, 2 rue Simone Iff, 75012 Paris

² CEREMADE, Université Paris Dauphine, Place du Marchal Lattre de Tassigny 75775
Paris

Keywords: *Optimal reconstruction, doppler velocimetry, inverse problems*

Doppler ecography is one of the most commonly used measurement modalities of blood flow in clinical applications. It is cheap and non-invasive. A number of decisions are made based on this kind of measurement. Of the available data, only a small portion is actually used in order to infer useful parameters characterising the blood flow and the quantities of interest.

Based on the theoretical results in [1] and the methods proposed in [2], a numerical method is proposed in order to reconstruct the 3D flow in realistic geometries starting from doppler velocimetry data. Ultrasound measurements are modeled. These can be seen, with a good approximation, as linear forms applied to the flow, so that the problem can be formulated as follows: given a set of linear forms applied to the flow and perturbed by noise, what is the best way to reconstruct the flow?

A mathematical analysis is shown. In order to assess the performances of the proposed method some numerical experiments are proposed, on synthetic geometries and in a more realistic case, on patient carotid arteries data.

REFERENCES

- [1] Binev, Peter and Cohen, Albert and Dahmen, Wolfgang and DeVore, Ronald and Petrova, Guergana and Wojtaszczyk, Przemyslaw, *Data assimilation in reduced modeling*.SIAM/ASA Journal on Uncertainty Quantification, 2017.
- [2] Y. Maday, O. Mula, A.T. Patera and M. Yano, *The Generalized Empirical Interpolation Method: Stability theory on Hilbert spaces with an application to the Stokes equation*, CMAME, 2015