

## FICTITIOUS DOMAIN DECOMPOSITION TECHNIQUE FOR RECOVERING MISSING BOUNDARY DATA: GROUNDWATER FLOW EQUATION

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**Summary.** In this paper, we consider an inverse problem known as missing boundary data recovering. We assume that a transient groundwater model is given in a computational domain with overspecified data on a part of the boundary and missing data on the other part. Classical approaches use a least-squares formulation which requires some regularization tool to solve this ill-posed problem. Here, we consider an approach based on an energy norm defined from two well-posed problems, which appears to be self-regularizing [2, 1]. There are several ways to minimize the energy norm. We follow the method introduced in [4] for the steady-state case, whereas we consider here a transient case. The idea is to write the first-order optimality conditions as an interfacial problem [3]. At each time step, we apply a preconditioned iterative gradient algorithm, which appears to be very efficient. Numerical experiments illustrate the robustness of the method, even for a noisy singular test case.

### References.

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