

# A high order MPM for 2-phase problems

Elizaveta Wobbles<sup>†</sup>, Cornelis Vuik<sup>†</sup> and Vahid Galavi<sup>‡</sup>

<sup>†</sup> Delft Institute of Applied Mathematics (DIAM)  
Delft University of Technology (TU Delft)  
Mekelweg 4, 2628 CD Delft, The Netherlands  
e-mail: E.D.Wobbles@tudelft.nl, C.Vuik@tudelft.nl

<sup>‡</sup> Unit GEO: Soil & Structure  
Deltares  
Boussinesqweg 1, 2629 HV Delft, The Netherlands  
e-mail: Vahid.Galavi@deltares.nl

## ABSTRACT

The material point method (MPM) has successfully been applied to a variety of geotechnical problems involving large deformations. However, the classical MPM suffers from a number of drawbacks, such as ‘grid crossing’ and quadrature errors, which can strongly influence the simulation results [1-2]. In [3] a high order version of the method has been proposed as a possible solution to these issues. The modified method combines quadratic B-spline basis functions with a reconstruction based quadrature rule, and shows great potential for one-dimensional 1-phase benchmarks. In order to bring the approach closer to real life geotechnical problems and accordingly refine it, we extend its range of applicability to multiphase materials. The performance of the method is investigated based on a number of one-dimensional 2-phase large deformation boundary value problems.

## REFERENCES

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